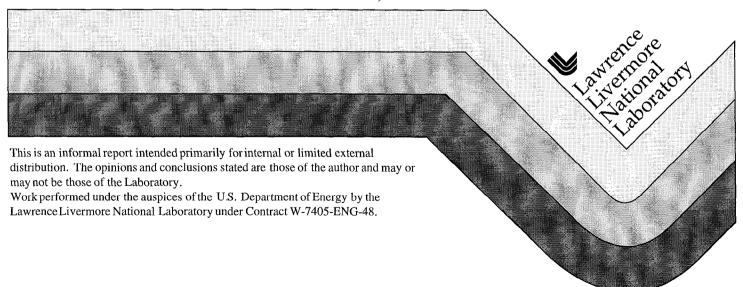
Grazing Incidence Liquid Metal Mirrors (GILMM) as the Final Optics for Laser Inertial Fusion Energy Power Plants

R. W. Moir

June 25, 1999



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Grazing incidence liquid metal mirrors (GILMM) as the final optics for laser inertial fusion energy power plants

R. W. Moir

Abstract

A thin film of liquid metal serves as a grazing incident liquid metal mirror (GILMM) for robust final optics of an inertial fusion energy (IFE) power plant. The amount of laser light the mirror can withstand, called the damage limit, of a sodium film 85° from normal arbitrarily set by surface temperature rise of 200 °C to limit liquid ablation is 57 J/cm² normal to the beam for a 20 ns pulse and 1.3 J/cm^2 for a 10 ps pulse of 0.35 µm light. Liquid aluminum can handle 106 J/cm^2 . The damage limit actually should be set by avoiding liquid ablation due to the rapid surface heating which is expected to result in even higher temperatures rises than 200 °C and even higher power densities. The liquid surface is kept flat to the required accuracy by a combination of polished substrate, adaptive optics, surface tension and low Reynolds number, laminar flow in the film. The film's substrate must be polished to $\pm 0.015 \, \mu m$. Then surface tension keeps the surface smooth over short distances (<10 mm) and low Reynolds number laminar flow keeps the surface smooth by keeping the film thickness constant to less than ± 0.01 µm over long distance >10 mm. Adaptive (deformable) optics techniques keep the substrate flat to within $\pm 0.06 \,\mu m$ over 100 mm distance and $\pm 0.6 \,\mu m$ over 1000 mm distances. The mirror can withstand the x-ray pulse when located 30 m away from the microexplosions of nominal yield of 400 MJ (50 MJ x rays) when Li is used but for higher atomic number liquids like Na and Al there may be too high a temperature rise forcing use of other x-ray attenuation methods such as xenon gas, which may be needed for first wall protecting anyway. The cumulative damage from neutrons causing warpage of the liquid film's substrate can be compensated by adaptive optics techniques giving the mirrors long life, perhaps 30 years. The GILMM should be applicable to both direct and indirect drive and pulse lengths appropriate to slow compression (~20 ns) or fast ignition (~10 ps). Experiments are discussed to verify the predicted damage limit and required smoothness.

Table of contents	
Introduction	3
System layout	4
Damage limit theory	7
Candidate liquids	8
Optical penetration and sound travel time effects	13
Theoretical basis for smooth film flow	14
Stability of the flowing film	17
Required smoothness of the liquid film and metal substrate	24
Flow rate control	26
Meniscus effects	26
Variation in surface tension and viscosity with temperature effects	27
Design of cooling system	28
Vibration damping system	29
Energy in vibrations	30
Active pointing system	31
Differential heating	31
Dry out	31
Neutron effects	32
X-ray effects	33
Debris protection	34
X-ray protection by gas	35
Blast effect on mirror deflection and mitigation	35
Optical alignment	36
Experimental test apparatus	36
Conclusion	37
Acknowledgments	37
References	38

Introduction

Metal mirrors have long been used in optics but for wavelengths of interest for laser IFE of 0.25 to 0.35 μm, grazing incidence (≈85° to normal) is needed to reduce absorption. Bieri analyzed a grazing incidence metal mirror (GIMM) and found aluminum could handle 18 J/cm² normal to the beam which is 1.5 J/cm² on the film¹. His design was used for the Prometheus² (Fig. 1) and Sombrero³ (Fig. 2) laser IFE power plants studies. Sombrero had mirrors at 6° grazing at 30 m of normal cross section of 1 m x 0.43 m with a mirror 1 m wide and 4.1 m along the slope direction. There were 60 beams totaling 3.6 MJ or 60 kJ/beam. The 60 kJ over 4.1 m² gave an intensity of 1.5 J/cm² on the film (14 J/cm² normal to the beam). At 50 m, the distance to the first conventional optics, the 14 J/cm² drops to 5 J/cm² damage limit on this conventional optics. A problem however, with the designs is that flaws as small as ~1 µm "looks" locally like normal incidence (~14 J/cm²) which far exceeds the damage threshold of 1.5 J/cm². That is, local absorption of heat would cause a small flaw to grow from shot to shot quickly leading to failure. If the surface were composed of a thin liquid metal film (grazing incidence liquid metal mirror or GILMM), surface imperfection would heal due to surface tension and due to fresh flowing liquid. If dust or other contaminant should land on the surface it will be slowly swept away (~100 s to move 1 m down the mirror). Melting and even evaporation is not a problem. The surface must flow slowly enough so that no shear flow instabilities cause a surface ripple. Heat must be removed from the back by conduction, not convection at the slow flow rates required to avoid surface ripple. There was previous mention in the literature of using liquid metal surfaces for laser fusion mirrors by Hovingh et al. in 1973⁴ and by Baird and Anderson in 1975⁵. Liquid metals (mercury) have already found application in telescopes based on a thin (~1 mm thick), 2.7-m diameter slowly rotating pool supported on an air bearing to form a parabolic mirror⁶.

The GILMM might last the life of the plant (>30 y) being limited by damage to the substrate. The second optical element which is out of the line of sight of the microexplosion can be of conventional optics design, e.g. dielectric coatings or refractive or diffractive SiO_2 . An alternative concept for final optics is use of SiO_2 operated so hot (~400° C) that damage is annealed continually. It is not known how long such materials can continue to serve as quality optics. GILMM appear

to be a complete solution to the final optics, being radiation hard to both neutrons and x rays, having long service life of >30 years and acceptable cost while being able to deliver high quality laser light to the target. Some or all of the final focusing can be accomplished with the GILMM by curving the substrate surface and using adaptive optics. The ideas presented in this paper might find application in making low cost telescope mirrors. Another application of GILMM might be final optics in laser fusion propulsion of space craft⁸. In space a slowly rotating set of GILMMs can function as discussed in this paper.

System layout

The final optics in two designs using direct drive are shown in Fig. 1 and 2. The angle of the beam lines (where 0° is horizontal and 90° is vertical) is up 67° in Fig. 2 (the mirrors are 5° steeper so are sloped up to 72°). In the lower half of the chamber the mirrors are sloped 5° less steep so the mirrors there are sloped up to only 62°. The distance to the final optics is 20 m in Fig. 1 and 30 m in Fig 2. For our examples we will use 30 m as well. The cross section of the beam in Figure 2 is 1 m by 0.43 m. The "foot print" on the 84° grazing incidence mirror is then 1 m by 4.1 m in the direction down the slope.

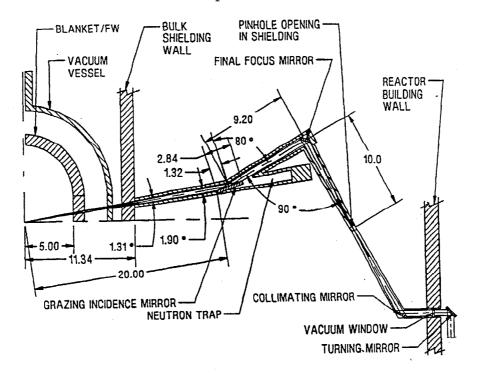


Fig. 1. Final optical elements in the Prometheus reactor design

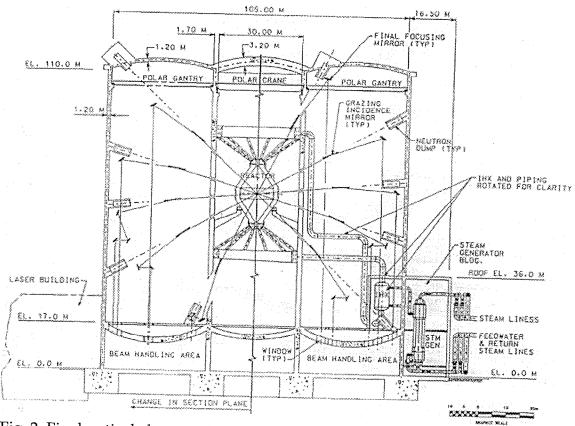


Fig. 2. Final optical elements in the Sombrero reactor design using GIMM. With GILMM the laser would hit the top side of the mirror rather than the underside as in GIMM, practically like turning this figure upside down.

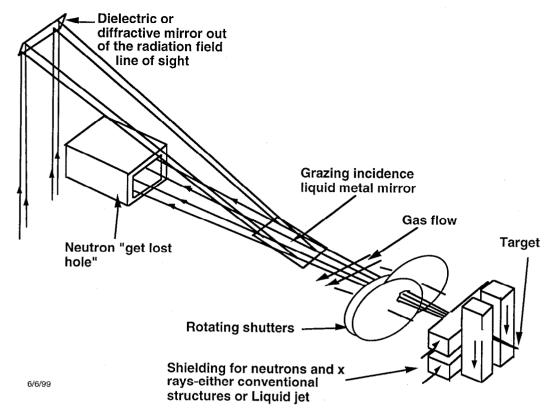


Figure 3. Typical optics layout showing key protection features.

Examples of optical layouts are given in Fig. 3 showing shutters and gas flow to keep debris from reaching the GILMM. Dielectric mirrors are shown based on present day practice which should be applicable out of the radiation environment but diffractive optics might be used as well.

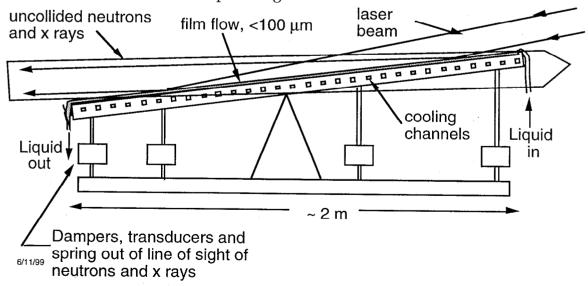


Fig. 4. Grazing incidence liquid metal mirror (GILMM)

A schematic of GILMM is shown in Fig. 4. The surface shape is controlled by methods of adaptive optics where servos turn a screw connected to a spring in order to vary a force pushing or pulling at as many places as necessary on the back of the mirror. The adaptive optics with servos are intended to correct for changes in shape over minutes or hours or longer; however, with piezo-electric transducers, beam pointing from shot to shot can be accomplished if needed in times of <0.1 s. The liquid is fed in at the top of the inclined plane with care so that the feed rate is constant across the mirror and disturbances are minimal. Small variation in entrance conditions will smooth out as the liquid flows down the plane. The liquid must wet the surface at all times. If dry out occurs for some reason, vapor deposition methods could be used to recoat, however, this would require a plant shut down which should be avoided if at all possible and therefore is a serious concern that will need research. Heat deposited by the laser, x rays and neutrons must be removed from the back by conduction, not convection at the slow flow rates required to avoid surface ripple. The servos and robotics for the GILMM can be out of line of sight of neutrons and x rays. The first and only structures to "see" uncollided neutrons will be the GILMM at 30 m distance from the shot point. There is reasonable hope the mirrors can last the life of the plant. There will be need for a pump (EM pump with no moving parts) and filter system to circulate the liquid metal and keep it clean.

Damage limit theory

The light pulse on the surface causes a temperature rise until some effect sets a limit we will call the damage limit light flux in J/cm^2 . R_S and R_p are the reflectivities for the case where the electric field is parallel and perpendicular to the plane from Ref. 9 and 1.

$$R_S = \frac{u^2 + v^2 - 2u\cos\phi + \cos^2\phi}{u^2 + v^2 + 2u\cos\phi + \cos^2\phi}$$
(1)

$$R_{P} = R_{S} \cdot \frac{u^{2} + v^{2} - 2u\sin\phi\tan\phi + \sin^{2}\phi\tan^{2}\phi}{u^{2} + v^{2} + 2u\sin\phi\tan\phi + \sin^{2}\phi\tan^{2}\phi}$$
(2)

where u and v are defined as:

$$2u^{2} = (n^{2} - k^{2} - \sin^{2}\phi) + [(n^{2} - k^{2} - \sin^{2}\phi)^{2} + 4n^{2}k^{2}]^{1/2}$$
(3)

$$2v^{2} = -(n^{2} - k^{2} - \sin^{2}\phi) + [(n^{2} - k^{2} - \sin^{2}\phi)^{2} + 4n^{2}k^{2}]^{1/2}$$
(4)

Where n and k are the frequency (wavelength) dependent refractive index and extinction coefficient of the liquid metal. The angle of incidence relative to the normal is ϕ and the electric field is polarized in the direction of the plane or perpendicular to the plane. The temperature rise at the surface, ΔT is given next.

$$\Delta T = \frac{2(1 - R)q_{beam}}{k_T} (\frac{\alpha_T t}{\pi})^{1/2}$$
 (5)

$$\alpha_T = \frac{k_T}{\rho c} \tag{6}$$

Where R is the reflectivity, q_{beam} is the power density of the optical beam on the metal surface, t is the time duration of the pulse, ρ is the density of the metal, α_T is the thermal diffusivity, k_T is the thermal conductivity and c is the heat capacity of the liquid metal. The skin depth or optical penetration depth is discussed in the section after the next one on effects of absorption and heating.

Candidate liquids

The choice of material for GILMM will be based on the damage limited heat flux and ease of handling. The mechanism that sets the damage limited heat flux is thought to be avoiding liquid ablation (spall) caused by the sudden heating (isochoric heating) and subsequent rapid expansion. The surface temperature rises monatonically until the end of the pulse. We arbitrarily set 200 °C as a measure of the damage limited heat flux until liquid ablation calculations are performed with hydro codes (ABLATOR 10 , for example). For comparison Bieri found a temperature rise limit of about 100 °C set by surface distortion (strain beyond the elastic limit for Al at room temperature). The light intensity at 0.35 μm for 200 °C temperature rise is given in Table 1 for a number of candidate liquids. Liquid lithium and mercury are possible but marginal especially when it comes to the short pulsed ignitor beams. Sodium or even aluminum may be the best choice as will be discussed further on. For the compressor beams the damage limit of GILMM is so high that the limit will be set by the optics that

follow out of line of sight of neutrons. This is likely even for the ignitor beams. The peak pressure, P, given in Table 1 is the Gruneisen pressure without any hydro motion, that is $p=\Gamma E/V$ where Γ is the Gruneisen parameter (usually near unity). The energy is deposited at the surface in a volume V. As the surface heats up, expansion occurs at the speed of sound so the pressure falls short of the values given in Table 1. These need to be calculated with a hydro code.

The reflectivity varies with angle as shown in Fig. 5 and with wavelength shown in Fig. 6 and 7. Clearly, we can see the importance of orienting the mirror so that the electric field is in the plane of the film. Commonly in inertial fusion the intense portion of the laser pulse is 8 to 10 ns long. However, it might be as long as 20 ns if a slow compression is used to make a dense cold core for fast ignition. Therefore, for our examples we assume a typical pulse is 20 ns long or in the case of fast ignitor 10 ps¹¹. The pulse length at the mirror might be much longer than this 10 ps. The results can easily be scaled to different pulse lengths. The allowed intensity scales as square root of the pulse length. The highest intensity allowed is for liquid Al, however, its high melting point of 660 °C suggest use of liquid Na or Li may be more practical with their melting points of 98 and 179 °C. Hg and Pb have considerable lower damage threshold. Mercury has a low vapor pressure at low temperature and will not react with Flibe. Li and Na have the additional advantage, their oxides and fluorides are dense enough to sink rather than form a (slag) that might interfere with reflection and make clean up harder. Wetting is a serious issue. Lithium should be able to wet steel once the oxide has been removed, which can be done a number of ways including submersing in Li at 600 °C for a few hours 12 to remove the oxides. Similar properties should apply to other alkali metals such as sodium.

Table 1

Damage limit for 20 ns pulses for a 200 °C surface temperature rise

	Tmelt	Pressure	e, Torr,	Laser fluence		Peak	Laser	Mirror area
	°C	·		on mirror		pressure,	fluence	for 60 kJ per
			:	(85°), J/cm ²		GPa	transverse	beam, m ²
		@ Tmelt		(absorbed)		9	to beam,	
		+ 100°C,	+300°C				J/cm ²	
Al	660	10 ⁻⁶	1· 10 ⁻⁴	9.2	(0.064)	2.1	106	0.65
Na	98	1.2.10-4	3.10-1	5.0	(0.025)	0.16	57	1.2
Ga	30	4 ⁻ 10 ⁻²⁶	4.10-15	2.4	(0.022)	0.4	28	2.5
Li	179	2·10 ⁻⁶	3.10-3	0.67	(0.025)	0.8	7.7	9.0
Hg	-39	2. 10 ⁻²	3.10	0.53	(0.010)	0.3	6.0	11
Pb	328	7.10-7	1·10 ⁻³	0.33	(0.013)	0.7	3.8	18

Al(solid) Sombrero³

1.5

14 4.1

The Sombrero design as discussed in the introduction had a mirror area of 4.1 m² with a laser intensity on the mirror of 1.5 J/cm². From the last column of Table 1 we can compare the area of GILMM with the various liquid metals to the area of GIMM of Sombrero of 4.1 m². Aluminum stands out and sodium is pretty good. Lithium is larger by a factor of two. The damage limit scales as (pulse length)^{0.5}, so that a 10 ps pulse could only handle a factor of 45 times less energy for the same surface temperature rise. If the ignitor pulse at the mirror had not fully compressed but rather were 200 ps long there, then the damage limit would be reduced by a factor of 10 from those in Table 1. For the compressor beams the damage limit of GILMM is so high that the limit will be set by the optics that follow out of line of sight of neutrons. This is likely even for the ignitor beams.

Reflectivity of liquid mercury

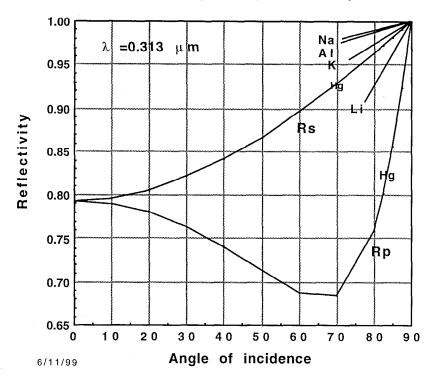


Figure 5. Reflectivity versus angle of incidence for mercury. The curve labeled $R_{\rm s}$ has the electric field parallel to the surface and $R_{\rm p}$ has a component of the electric field perpendicular to the surface. For comparison the reflectivities for other liquid metals are shown.

There are a number of effects that contribute to absorptance (1-R) discussed by Bieri¹ that have been neglected and need to be added to the analysis here.

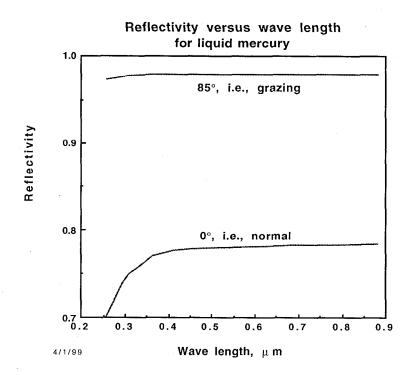


Figure 6. Reflectivity versus wave length for mercury

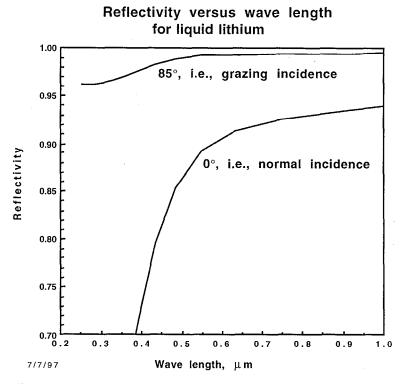


Figure 7. Reflectivity versus wave length for liquid lithium

The performance of GILMM might be strongly effected by wavelength of possible lasers. For Li the damage limit for 1/4 and 1/3 μ m light is about the same but is about 2.8 times higher for 1/2 μ m light and 7.3 times higher for 1 μ m light compared to 1/3 μ m light.

Optical penetration and sound travel time effects

The question comes up of how deep is the optical penetration compared to the thermal diffusion distance for two reasons. Liquid surfaces are not characteristic of the bulk for the first few atomic distances into the interior and the surface may have some contaminants on it. Does either of these effects matter? Also the peak pressures shown in Table 1 are diminished by a relief wave traveling at the speed of sound during the heating pulse so as to reduce the peak pressures and hence the peak tension as well. These effects are illustrated in Table 2. The optical penetration depth is not many atom layers into the interior for most of the candidate liquids at 85° incidence. This may be a reason to change to 80° in future studies. For all cases the distance heat diffuses during the pulse is long compared to the optical penetration distance. For pulse lengths of 20 ns, sound waves can diminish the pressure build up due to the heating during the pulse to a great extend but only somewhat for the 10 ps pulses characteristic of fast ignitor beams.

The thermal diffusion length, $\ell_{\it diff}$ is

$$\ell_{diff} = (t \frac{k_T}{\rho c})^{1/2}$$

where the symbols are defined in Eq. 5 and 6.

Table 2
Optical penetration and sound travel times

	Optical	Thermal diff. di	Distance sound		
	penetration, 85°		travels, µm in		
	incidence, Å,	20 ns pulse	10 ps pulse	20 ns	10 ps
Al	6.9	1.2	0.028	9.2	0.064
Na	24	1.1	0.025	50	0.025
Ga	5.5	0.54	0.012	40	0.02
Li	20	0.67	0.015	40	0.02
Hg	9.7	0.30	0.0066	29	0.015
Pb	7.7	0.46	0.010	36	0.018

 $(1 \mu m = 10,000 \text{ Å})$

Theoretical basis for smooth film flow

The film must be sufficiently thin so that viscous forces overcome shear effects that lead to wave buildup. According to theoretical analysis, if the Reynolds number is below the critical value, disturbances will damp rather than grow. Short wave length disturbances damp quicker than long wave disturbances and when surface tension (which is unimportant at long wavelengths >100 mm) is included, short wave disturbances damp even more quickly. All this suggests that impulses delivered at 5 to 10 Hz or higher may not be a problem as will be discussed later. That is, a disturbance might damp out by the next pulse. Heat removal, discussed later, by subsurface cooling channels will keep temperature variation over the film surface small.

The film flow Reynolds number from Ref. 13 is given in Eq. 7, where ρ is density, h_0 is the film thickness, η is viscosity and θ is the angle of the film flow plane.

$$Re = \frac{\rho^2 g h_0^3 \sin \theta}{2\eta^2} \tag{7}$$

Critical Reynolds number for stability of long wave length disturbances:

$$Re_{crit} = \frac{5}{4}\cot\theta \tag{8}$$

The surface flow speed Uo is

$$U_0 = \frac{\rho g h_0^2 \sin \theta}{2\eta} \tag{9}$$

where the average flow speed is $\frac{2}{3}U_0$

The Weber number is useful to show when surface tension effects might be important.

$$We = \frac{\sigma}{\rho g h_0^2 \sin \theta} \tag{10}$$

For lithium, whose viscosity, η , is 0.41 mPa•s and surface tension, σ , is 0.35 N/m, we get a Weber number, We, of 4000 for θ = 10° and 100 μ m film thickness. Surface tension effects are extremely strong over dimensions comparable to the film thickness of interest. Disturbances with dimensions up to a few centimeters will be reduced strongly by surface tension but beyond a few centimeters surface tension is ineffective as will be discussed below and illustrated in Fig. 8 and 9.

The film thickness required for stable flow (Reynolds number is less than the critical Reynolds number from Eq. 8) is plotted in Fig. 8 and 9 for liquid Li and Na^{13} with the geometry and variables defined in Fig. 10. We can see that if the film is <100 μm , then the surface should be smooth for a 10° slope for Na. What limits the minimum thickness is not known but maintaining wetting may be a limitation to thickness.

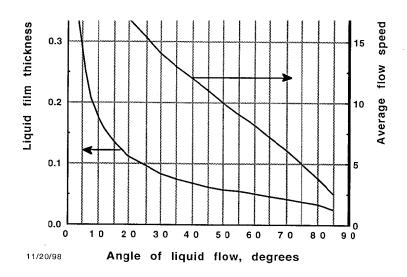


Fig. 8. Liquid film thickness and speed for laminar flow of lithium.

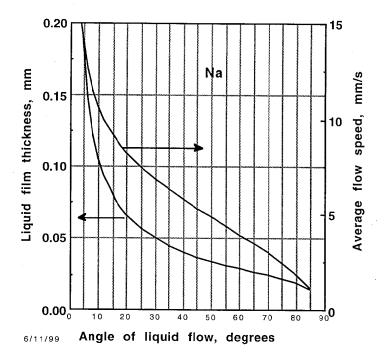


Fig. 9. Liquid film thickness and speed for laminar flow of sodium.

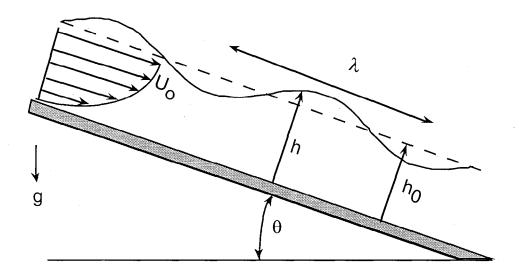


Fig. 10. The variables describing film flow down an inclined plane are shown above.

In the Sombrero study with direct drive, employing 60 beams, the steepest beam enters at 67° (where 90° would be directly overhead). With 5° grazing, the mirror would be inclined to 72°. From Fig. 8 and 9 we see the thickness of film must be $<40 \ \mu m$ for Li and 25 μm for Na to avoid waves. Experiments will be needed to see if stable thin flowing films can be made especially for steep slopes.

Stability of the flowing film

When the film thickness is less than that shown in Fig. 8 and 9, the flow is laminar and stable according to the theory to long wavelength disturbances. We can imagine even with perfectly smooth steady flow, disturbances can be initiated by events such as laser heating of the surface at 5 to 10 Hz rate including uneven heating, acoustic motion due to gas (target debris) striking the surface, heating by neutrons and so forth. The metal backing is assumed to be fastened with damped actuators at multiple places behind the flowing surface. In the discussion to follow we estimate the rate of damping of disturbances of the liquid surface. We assume any disturbance can be decomposed into sinusoidal disturbances as shown in Fig. 10. From the analysis of Howard 13 we find the growth rate of a disturbance of wavelength λ is given by γ :

$$\gamma = \frac{2\alpha^2}{3\sin\theta} \left[\left(\frac{6}{5} R\sin\theta - \cos\theta \right) - \frac{\Gamma}{gh^2} \alpha^2 \right]$$
 (11)

$$\alpha = \frac{2\pi h}{\lambda} \tag{12}$$

where Γ is the surface tension. For the sake of the discussion to follow, we assume there is a disturbance produced by external factors such as the acoustical response of the laser heating or the gas shock that hits the surface of the mirror. The disturbance can be Fourrier analyzed into sinusoidal components with a given wavelength. This is the meaning of disturbance we are using. The growth exponent, G, is defined as growth of the disturbance, e^G , where for a 1 m distance down the flow path G is given as:

$$G = \frac{U_0}{h} \gamma \left(\frac{100}{2U_0}\right) = 50 \frac{\gamma}{h} \tag{13}$$

where Uo is the surface speed and γ is the growth rate. Two cases are treated, one for 5 degree slope and the other for 70 degree slope to illustrate the range of parameters involved including the direct drive option. Fig. 11 and 12 shows the 5 degree case in linear and a log plot for Li. Fig. 13 and 14 show the 70 degree case for Li. Sodium is shown in Fig. 15 and 16. When the film is thicker than that shown in Fig. 8 and 9 disturbances grow. Disturbances of wavelength below about 10 cm for 5 degrees and below 5 cm for 70 degree slopes are strongly damped due to the effects of surface tension. The damping rate becomes small for wavelengths longer than 10 cm for a 5 degree slope and longer than 5 cm for a 70 degree slope. Isochoric heating will set up sound waves that will travel from the mirror front to the back in times of 5 µs and from one end to the other in about 1 ms. Since there is no net momentum in isochoric heating expansion, these sound waves should simply damp out after some number of transits. For a 5 degree slope from Fig. 8 we see a film <0.3 mm will be stable and flow at a surface speed of 35 mm/s for Li. However the waves travel at twice the surface speed giving 70 mm/s. In an interpulse time of 0.17 s for 6 Hz the distance a wave travels is <12 mm. To have one e-fold damping would correspond to a G value at 1 m of -83 (1/0.012 = 83), which is obtained only for wavelengths of disturbances of 20 mm or less as can be seen in Fig. 8. Stated another way a 20 mm wavelength disturbance will damp (1/e) in 0.17 s. A 10 cm wavelength disturbance will damp (1/e) in 1 m or $14 ext{ s}$ $(1 ext{ m}/70 ext{ mm/s})$. A 20 cm disturbance (G=-0.2 at 1 m) would damp (1/e) in a distance of flow of 0.5 m or 71 s. If there

is a driving force for surface displacement disturbances over distances greater than 10 cm, there may be a problem because these disturbances may damp to slowly. Thinner films than 0.3 mm will damp disturbances more quickly. For the 70° slope (Fig. 13 and 14), the damping rates are much smaller. More analysis and experimentation will be needed to prove surfaces can be kept sufficiently smooth for the application to IFE. Other than acoustical forces and vibrations from the mounting system, both of which can be virtually eliminated by design, we are hard pressed to find a mechanism to produce surface disturbances. Next we discuss the required smoothness.

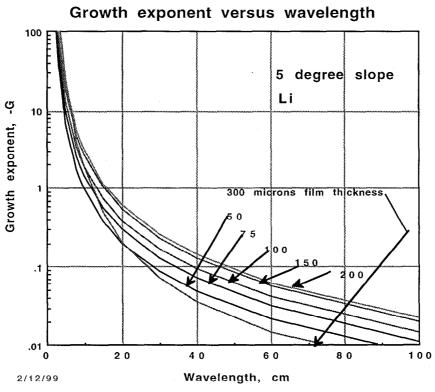


Fig. 11. Growth exponent (growth ∞e^G) versus wavelength for 5 degree slope film flow with liquid lithium plotted on a log graph for 1 m flow path (Howard Ref. 13). Note there is a thickness of the film that is the most stable or has the largest damping.

Growth exponent versus wavelength

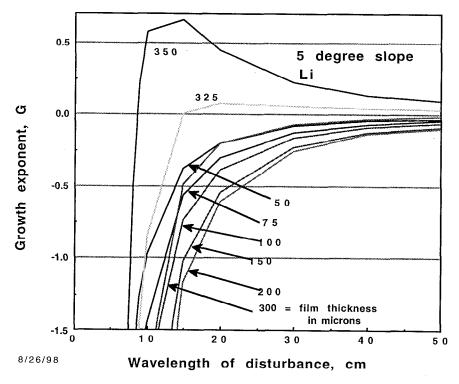


Fig. 12. Growth exponent (growth $\propto e^G$) versus wavelength for 5 degree slope film flow with liquid lithium plotted on a linear graph for 1 m flow path (Howard Ref. 13). Note there is a thickness of the film that is the most stable or has the largest damping.

Growth exponent versus wave length of disturbance

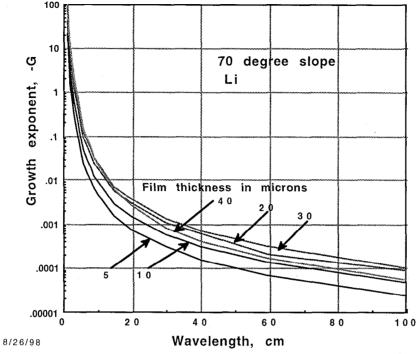


Fig. 13. Growth exponent versus wavelength for 70 degree slope film flow with liquid lithium plotted on a log graph for 1 m flow path.

Growth exponent versus wavelength

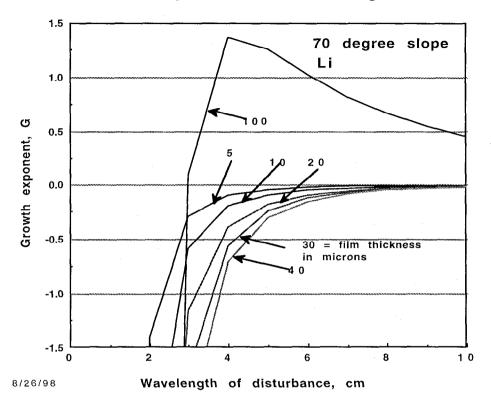


Fig. 14. Growth exponent versus wavelength for 70 degree slope film flow with liquid lithium plotted on a linear graph for 1 m flow path.

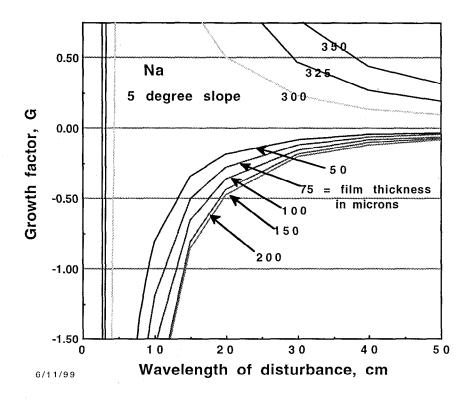


Fig. 15. Growth exponent versus wavelength for 5 degree slope film flow with liquid sodium plotted for 1 m flow path.

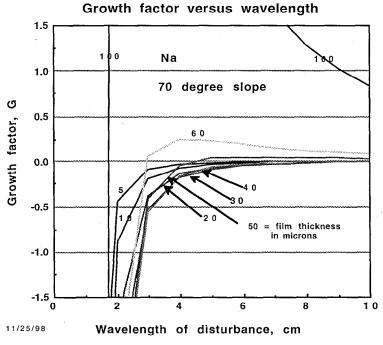


Fig. 16. Growth exponent versus wavelength for 70 degree slope film flow with liquid sodium plotted for 1 m flow path.

Required smoothness of the liquid film and metal substrate

A simple analysis is done to show how smooth the liquid surface must be. Suppose there is a sinusoidal surface ripple of $\pm\Delta h/h$, over a wavelength, λ , then the angle of reflection will be spread by $\pm 4\pi\Delta h/\lambda$ as shown in Fig. 17. For a 30 m distance and a displacement of \pm 0.25 mm at the target, which is about 10% of a typical capsule radius, we can tolerate a value of \pm 0.066 μ m (\pm 660 Å) for a wavelength of 100 mm. This is a pointing accuracy of \pm 8.3 μ radians. The surface tension will be helpful in keeping surface disturbances small over short distances <10 mm. Over long distances (>10 mm) the backing plate must be kept flat to the parameters in Table 3.

Table 3
Surface disturbance allowed over the liquid metal mirror

Distance along	Allowed perturbation, $\pm \Delta h_0$, μm
mirror, λ, mm	
1	±0.00066
10	$\pm 0.0066 = 6.6 \text{ nm} = 66 \text{ Å}$
100	$\pm 0.066 = 66 \text{ nm} \sim \lambda_{\text{laser}}/4$
1000=1 m	±0.66
5,000=5 m	±3.6

The "polish" will have to be < $\pm 0.0066~\mu m$ over distance of < 10 mm which is brought about by surface tension. Over distances of 10 mm or more the substrate polish must be $\pm 0.007~\mu m$. Surface tension may relax this somewhat and should be the object of more analysis. We will assume the figure is twice this or $\pm 0.015~\mu m$ when surface tension is fully included. We can use adaptive optics to hold the substrate to $\pm 0.66~\mu m$ over 1 m distances. In summary, a substrate

polish of $\pm 0.015~\mu m$ ($\pm 150~\text{Å}$ or $\lambda/20$) with adaptive optics should meet the requirements to hit targets to within $\pm 0.25~mm$ (about 10% of the capsule radius) at 30 m. To get a pointing accuracy of $\pm 25~\mu m$ ($\pm 0.83~\mu radians$) should this become necessary would require a polish of the substrate of $\pm 0.0015~\mu m$ ($\pm 15~\text{Å}$). The diffraction limited spot size is about 9 μm .

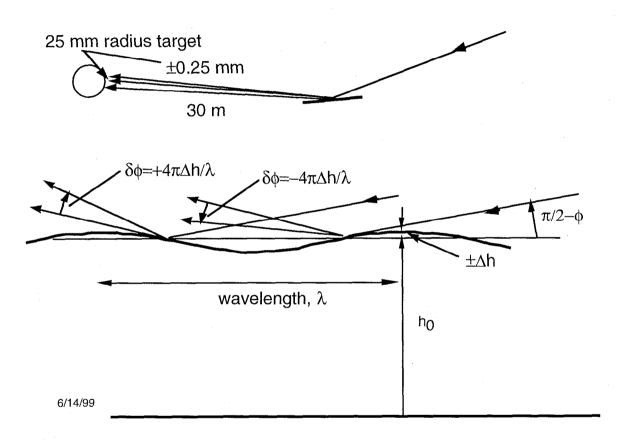


Fig. 17. A surface ripple on the liquid will cause a smear in the focal spot at the target by $\pm 4\pi\Delta h/\lambda$ in radians.

An experiment is needed to verify surface smoothness. It could be done with any liquid metal and any laser wavelength using the Reynolds number to extrapolate to other liquids. Another experiment is needed to verify the reflectivity at the high intensity shown in Table 1. This experiment would be preferably done with Na and the correct optical wavelength so that no extrapolation by theory would

be required assuming Na turns out to be preferred. Na seems to be favored at the present.

Flow rate control

Uniform flow rate will be important to keep the surface adequately smooth. The thickness varies with the third root of the flow rate as can be seen from Eq. 7. The flow rate for the 5° slope case and 300 μ m is 8 cm³/s and for the 70° slope case and 40 μ m film is 0.24 cm³/s. A Δh of \pm 0.6 μ m over a time of 36 seconds would be allowed from Table 2 for a surface wave length of 1 m down the slope of the mirror forcing the flow rate to vary by no more than \pm 14 % over 36 s. The spatial feed at the top of the mirror must be uniform to within a flow rate of \pm 7 % over distances of 50 cm or so. Irregularities over 10 cm or less will be smoothed out by surface tension. The feed system requirements appear easily satisfied both spatially and over time.

Meniscus effects

The liquid can be constrained to flow down the slope and not over the edge by a lip of height higher than the meniscus height, h, or having an edge that does not wet.

$$h = \left(\frac{T}{\rho g \cos \vartheta}\right)^{\frac{1}{2}} \cot \beta \tag{14}$$

where T is the surface tension, β is the contact angle and θ the slope angle of flow. The lip needs to be only a few mm in most cases as can be seen from the Table 4 for the case of contact angle, β , equal to 45° .

Table 4
Meniscus height

Element	surface tension,	density,	meniscus	meniscus
	T, N/m	ρ , kg/m ³	heighth, h,	heighth, mm
			mm, 5° slope	70° slope
Al	0.52	2700	4.4	7.6
Bi	0.37	9780	2.0	3.4
Ga	0.735	5930	3.6	6.1
In	0.34	7280	2.2	3.7
Pb	0.438	11340	2.0	3.4
Li	0.383	534	8.6	14.6
Mg	0.563	1740	5.8	9.8
Na	0.206	970	4.7	8.0
Hg	0.465	14200	1.8	3.1
K	0.086	870	3.2	5.4
Water	0.073	1000	2.7	4.7

Another effect of the meniscus is to distort the liquid surface near the edge of the mirror. The shape of the meniscus is

$$y = he^{-\left(\frac{\rho g \cos \vartheta}{T}\right)^{0.5} x}$$
 (15)

The slope of the surface is

$$\frac{dy}{dx} = h(\frac{\rho g \cos \vartheta}{T})^{0.5} e^{-(\frac{\rho g \cos \vartheta}{T})^{0.5} x}$$
(16)

which for β =45° is $e^{-\frac{x}{h}}$. The allowed deflection to still hit the target is estimated to be $\Delta \varphi$ =0.25 mm/30 m=8.3 µradians; dy/dx=0.5 $\Delta \varphi$. This occurs for x=58 and 99 mm for sodium at 5° and 70° slope. The wall to hold the liquid for an 85° incident beam will obscure the edge of the mirror. For sodium this distance is 54 mm and 91 mm.

Variation in surface tension and viscosity with temperature effects

There is considerable analysis in the literature on the effects on flow of varying surface tension and viscosity with variations in temperature. These effects are more important for growth of waves but for our case where all waves are damped, the damping rate may changes somewhat but no new effects are expected. The temperature variation along and across the liquid film will drop to a low value during typical interpulse times (0.035 °C, see later section "Differential heating"). The fractional variation of surface tension and viscosity for sodium for a 0.035 °C temperature change is -1.73×10^{-5} and -1.6×10^{-4} near 100 °C.

Design of cooling system

The cooling system must not introduce significant temperature variations along the film flow because changes in viscosity will change the flow rates and hence the thickness and result in a surface ripple. Analysis will be needed to see how much temperature variation can be allowed. If there is a temperature variation in the liquid metal film due for example to cooling channels in the back of the substrate as shown in Fig. 4, there will be a change in the viscosity and density. Lower viscosity will result in higher flow speed locally but due to continuity the flow rate is fixed so the film thickness will drop locally producing a ripple in the surface. The flow per unit length across the mirror = feed rate = constant=2Uh/3 where U is given in Eq. 9.

$$\frac{\rho g h_0^3 \sin \theta}{2\eta} = const. \tag{17}$$

The variation in the film thickness, h, can be related to the variation in the ratio of viscosity to density.

$$\frac{\Delta h}{h} = \frac{\Delta(\frac{\eta}{\rho})}{3\frac{\eta}{\rho}} \tag{18}$$

From Table 3 we can allow Δh to be $\pm 0.00667~\mu m$ over distances of 10 mm, which might be a typical coolant channel distance. For a 100 μm thick film then $\Delta h/h < 0.0066/100 = 0.66 \times 10^{-4}$ we then require $\Delta (\eta/\rho)/\eta/\rho < 0.22 \times 10^{-4}$

From data on sodium we find $=9\times10^{-3}$ per degree The allowed $\Delta T < 0.0024$ °C variation on the surface over distance of 10 mm and 0.024 °C over distance of 100 mm.

In the section on differential heating we show the steady temperature rise of 0.002 °C is needed across a 100 μm film to transmit 0.025 J/cm² absorbed at 6 Hz. So we require the laser intensity does not vary by more than 100% over distances of 10 mm from shot to shot which seems easy to satisfy. The demands placed on the variation in the ΔT between the coolant channel and the film substrate to be no more than ± 0.002 °C seems challenging. Clearly, the above discussion indicates thermal management will have to be taken seriously as a design parameter.

The effect of viscosity variation on stability of the flow has been studied by Goussis and Kelly^{14, 15}. They find an extra stabilizing effect for surface heating of the film and cooling from the back of the film as in our case.

Vibration damping system

The mirror system needs to be shock mounted and critically damped so that vibrations excited by, for example, bursts of vapor coming up the beam line (i.e., acoustic vibrations) at the microexplosion pulse rate of 6 Hz or so will damp by the next shot in 1/6 s. It will be important to have such driving forces small and not be resonant with any natural frequencies that might set up a ripple pattern on the film. This means the natural frequency of all modes of the mirror must be greater than 6 Hz. The isochoric heating of the liquid surface by the laser and by x rays and the bulk liquid and substrate by neutrons are not expected to set up sustained vibrations because there is no net momentum transfer. As soon as the sound wave travels back and forth across the thickness of the mirror substrate of 10 mm or so a few times these vibrations damp out in times of tens of microseconds (several times the sound transit time). There are tens of thousands of transit times across the film and substrate combined. There will be internal reflections. The media will have damping in it. The support structure of the substrate will cause scattering of acoustic vibrations turning components into travel along the direction of the film flow with further damping. This subject can be analyzed further but looks likely to be no problem.

If there is some ablation of liquid or vapor, then there would be net momentum transferred to the substrate and mounting system, however we design to avoid ablation. Another driving force would be acoustic coupling through gas. This motion would be easily critically damped in times short compared to the interpulse time of $\sim 1/6$ s but still may set up standing waves on the liquid film. Therefore, we recommend keeping the gas at the mirror intentionally placed there to stop debris or from the debris itself at a very low pressure.

Energy in vibrations

From Table 1 for Na the laser energy incident on the liquid metal surface might be as high as $5 \, \mathrm{J/cm^2}$. The amount of laser light absorbed is $0.025 \, \mathrm{J/cm^2}$. The energy of vibration due to laser isochoric heating (24 Å penetration, 80 m/s vibration speed, an over estimate) is $0.8 \times 10^{-6} \, \mathrm{J/cm^2}$ and the kinetic energy in the flow for $100 \, \mu \mathrm{m}$ film and 10° slope is $0.5 \times 10^{-9} \, \mathrm{J/cm^2}$. More study is called for of the dissipation of the vibration in the liquid caused by laser heating and possible coupling to surface disturbances not sufficiently damped as to disrupt good reflectivity.

Active pointing system

Suppose the position of a target can accurately be injected to within a zone of ± 10 mm and be predicted by telemetrics to an accuracy of less than ± 0.25 mm. Can the GILMM at a distance of 30 m be turned by 10 mm or 0.3 mradians to an accuracy of ± 8.3 µradians (± 0.25 mm) in a time short compared to the interpulse time of 1/6 s for 6 Hz? The forces on actuators needed to do this are modest (~ 100 N or 20 pounds). The mounting of the GILMM must be critically damped and must have natural frequencies of vibration modes much faster than 6 Hz. Therefore it seems the mirror can be actively pointed for each target if desired and if this motion does not excite surface disturbances on the film.

Differential heating

The x rays and neutrons hit a distance in from the mirror edge as shown in Fig. 4., thus heating up and expanding that portion. This will tend to cause warpage which must be counter acted by the transducers. The warpage would be reduced if the x rays and neutrons hit the entire mirror and then the substrate would be expected to heat uniformly. The draw back of not collimating, though, is the intense heating of surfaces of the support struts and less so of their volumes. While the temperature at the surface of the liquid will increase 200 °C at the end of the laser pulse in our examples, it returns to its steady value in 0.2 μ s of about 0.035 °C above the temperature of the substrate for a 100 μ m film of Na for a laser beam of 5 J/cm² on the film (0.025 J/cm² absorbed) or 57 J/cm² transverse to the beam and 6 Hz. The steady temperature rise would only be 0.002 °C for the laser heating only, if the x rays were absorbed some other way. Neutron heating has been neglected here.

Dry out

It is essential the liquid film wets the substrate. If the surface becomes dry in spots, rivulets will form and surface ablation of the substrate can be expected. A method to wet once dry out occurs, for example, by vapor deposition may be needed. Hoffman and Potts have studied the wetting problem for lithium ¹⁶.

Neutron effects

Over long periods of time swelling of the substrate is expected and differential swelling will lead to warpage. As in the above discussion, there would be much less warpage if the neutrons illuminated the entire mirror rather than be collimated and expose just a footprint on the liquid surface. If the surface varies due to radiation damage on a local scale over distance of 10 to 100 mm by more than $\pm 0.015~\mu m$, then periodic resurfacing or replacement would be necessary because the film will also be distorted by a like amount. Over long distances (>100 mm), neutron induced warpage can be accommodated by the slow adaptive optics system. Sawan and Khater ¹⁷ estimate the flux of neutrons over 0.1 MeV on the mirror is $8.2 \times 10^{12} n \cdot cm^{-2} s^{-1}$ and is due mostly to direct source neutrons. Over a 30 year period at 80% capacity factor this would result in a fluence of $6.2 \times 10^{21}~n/cm^2$. More analysis is needed to prove the mirrors can last the life of the plant.

An extensive study of grazing incidence metal mirror (GIMM) was made by Bieri¹. He estimated the damage threshold for Aluminum GIMM at a laser energy of 1.5 J/cm² on the mirror surface for 85° from normal, which corresponds to 18 J/cm² normal to the beam. The lifetime of mirrors located at 30 m was estimated to be 3 years for 1000 MWe based on the effects of neutron damage causing surface roughness. A critical issue with GIMM was the necessity to avoid surface defects, or keeping small objects (>1 µm) such as dust from the surface because once appearing, the damage will grow and destroy the mirror. The damage mechanism is heat deposition causing the surface to exceed the elastic limit resulting in surface roughness. Further heat can cause melting and evaporation. These effects are cumulative. The lifetime of the GIMM will then be determined by the time for the first surface defect or debris to occur. Then the surface would need cleaning or repairing. Otherwise the mirror would then be useless. Frequent changeout of GIMM would be problematic in two ways. The cost of replacing the mirror and the down time in the replacement both have the effect of increasing the cost of electricity. Robotics will be necessary to quickly replace, locate, and align replacement mirrors. The liquid film added to the GIMM should extend the three year lifetime estimate perhaps to 30 years but just how long is left for further study.

X-ray effects

Xenon gas may be needed to protect the chamber and optics from x rays, and this, gas may be used in the beam tubes to stop debris. Without any gas protection, the burst of x rays will cause surface heating independent of angles of incidence for the mirrors located 30 m from the microexplosion. This has been estimated and the results are given in Table 5 for 50 MJ of x rays at 3 keV and 10 keV to illustrate the problem. To do the problem correctly we need the x-ray spectra, which for heavy ion targets is estimated ¹⁸ to radiate as a black body at 350 eV. At energy depositions below the vapor ablation we still are concerned with isochoric pressure causing expansion and a liquid ablation when the tensile wave "breaks" or exceeds the tensile strength of the liquid. For Li there is no problem but for much heavier elements there is a problem because we expect x ray intensities of 4.42 kJ/m² (0.44 J/cm²). The liquid at the surface finds itself under pressure due to the isochoric heating by x rays. The surface expands at the "jump off" speed, which is defined as

$$v_{jumpoff} = \frac{P_o}{\rho c} = \frac{\Gamma E_n}{\rho c} \tag{19}$$

where E_n is the volumetric energy density, c is the speed of sound, Γ is the Gruneisen parameter.

Table 5
Temperature rise due to x-ray burst

Element	Temperature rise, K		Isochoric		Jump off speed,	
			pressure, GPa		m/s	
	3 keV 10 keV		3 keV 10 keV		3 keV	10 keV
Li	0.5	0.04	0.002	0.0002	2.1	0.17
Na	185	5	0.16	0.005	67	1.9
Al	319	11	3.8	0.13	220	7.4
Ga	983	37	2.3	0.09	196	7.3
Pb	6300		25		1200	
Hg	6600	380	13	0.7	610	35

We need to know what pressure (which soon becomes tension) will result in liquid ablation or spall. It appears lithium will not spall, whereas Al likely will. Even if spall occurs, the surface will heal. Spall should be avoided or minimized but is not fatal. The above analysis should be redone for a calculated x-ray spectra from a direct drive capsule and from an indirect drive target and should use a hydro code calculation to determine the spall condition. The consequence of this analysis will be whether or not x-ray protection such as xenon gas will be needed.

Debris protection

The target debris and ablated liquid coming from the chamber that is directed towards the mirror before the shutter closes will constitute a surface contaminant on the liquid mirror if not stopped by the protective gas shown in Fig. 3. This should amount to about $1 \,\mu\text{g/cm}^2$ coming up the beam line at 30 m before the shutters close in 0.1 ms or $0.0004 \,\mu\text{m/shot}^{19}$ on the mirror and for 500 shots appropriate to film transit across a 2 m mirror before all liquid is replaced with new incoming liquid, 0.2 µm, which is less than a wavelength and less than the optical penetration depth as shown in Table 2 and therefore should cause no interference with the laser reflection. The problem here appears to be a long-term contamination of the liquid which sets the design requirement for clean up of the liquid. Impurity contaminates can be serious as they can segregate to the surface. Those systems are favored that have major contaminants sink as in lithium oxide or fluoride in lithium as opposed to lead oxides floating on lead for example. This contamination can be almost entirely avoided by flowing a dry clean inert gas in the beam tube to stop the debris from getting to the liquid metal surface. Suppose we assume ten times the density of xenon gas (10 mg/cm²) will effectively stop the 1 mg/cm 2 of debris. This would be 4.6×10^{13} atoms/cm 3 over 10 m or 12.9 mTorr. The density of this gas flow is so low that its effect on laser optical propagation is negligible. Experiments by Nilson et al. 18, showed laser propagation through Kr ~10 mg/cm² of 20 Torr•m over ~10 m distance with turbulent distortion of the focal spot <100 μm.

X-ray protection by gas

A high Z gas such as xenon can provide protection of optics from x rays if needed. This same gas provides protection from vapor and small droplets and other debris as discussed previously. We can expect 1/e reduction of 1 keV x rays with 0.14 Torr•m of Xe $(1.1 \times 10^{-4} \text{ g/cm}^2 \text{ or } 18.2 \text{ Pa•m})$. At 3 keV this becomes 1.8 Torr•m of Xe $(1.4 \times 10^{-3} \text{ g/cm}^2 \text{ or } 230 \text{ Pa•m}$. Large debris is moving slowly and will be stopped by the rotating shutters. Lehmberg at NRL predicts problems of propagating intense light through xenon gas at 0.248 µm but little problem at 0.3 μm and longer wavelength²⁰. The problem arises from a two photon resonance in Xenon near 0.248 µm causing a strong negative index of refraction change. The resonance is not so close in Kr as to be a problem. Other gases than Xenon can be considered. For the extra intense ignitor beams this needs examining and is still unresolved. There is a speculation that xenon can be introduced as a fog of droplets that passes over 90% of the laser light but by the time x rays return, the fog has turned into a gas that attenuates the x rays. The xenon gas must be fairly quiescent to avoid turbulence producing focal spot size problems. Experiments were carried out that give encouragement that xenon can be introduced without unduly enlarging or deflecting the spot size²¹ if special care is given to laminarizing the gas flow to reduce turbulent index of refraction dispersion. They got acceptable (<100 μm) focal properties with~20 Torr•m of gas, which will provide good protection from x rays.

Blast effect on mirror deflection and mitigation

The gas blast from the micro explosion can be largely decoupled from the mirror, however, some vapor impulse can be tolerated. Isochoric heating by neutrons and x rays do not impart net momentum, so, should not harm the focal properties. If ablation of liquid or vapor occurs there will be momentum imparted to the mirror. In either case the adaptive optics system with its spring mountings with transducers and dampers will be designed to have their natural frequencies higher than typical pulse rates of ~ 6 Hz and be close to critically damped. The blast has been estimated by Jantzen¹⁷ to have an impulse of 30 Pa•s at 3 m for a 400 MJ indirect drive heavy ion target. This impulse will diminish faster than $1/r^2$ especially with proper baffles. At 30 m an over estimate of the impulse would be 0.3 Pa•s. A mirror might have a mass of 140 kg. A suspension

system frequency of 60 Hz which would result in a negligible displacement of 5×10^{-7} µm. For grazing incidence this would displace the focal spot by the same amount. The focal spot tolerance might be \pm 250 µm. A Flibe droplet of 1 mm radius and speed of 1000 m/s would cause an impulse over the mirror of 1.3 Pa•s.

Optical alignment

The optical elements and adaptive optical corrections will have to periodically be corrected. This can be done by injecting special targets which are intended for beam alignment and not energy production. One target out of every 200 would hardly be missed. Then just one or a few beams can be fired onto this target and the position of the spot and its shape can be measured and corrections made. By this means all beams can be upgraded periodically. For 60 beams it would take at most about 0.5 hours to update each beam once and much less if several were done at the same time. The optical system required for these observations will occupy ports and need to be radiation hardened, however, high intensity on the optical surface is not needed. Even ion driven IFE will need an optical observation system for alignment purposes.

Experimental test apparatus

The GILMM concept can be tested in relatively simple low cost apparatus that is then brought to an appropriate laser for testing. Initial test in a glove box may be appropriate. A low power steady laser can be used to test the smoothness of the flow by looking at its reflected focal spot. If the flow has waves, the focal spot will oscillate. A high power density $(57 \, \text{J/cm}^2 \, \text{over 20 ns or } 2.9 \times 10^9 \, \text{W/cm}^2 \, \text{based on sodium from Table 1)}$ laser can test deliverability of high power into a reflected focal spot. For a focal spot size of >0.1 mm, the laser should have >4.9 mJ, > $2.2 \times 10^5 \, \text{W}$ for 20 ns. A schematic of such a test facility is shown in Fig. 18.

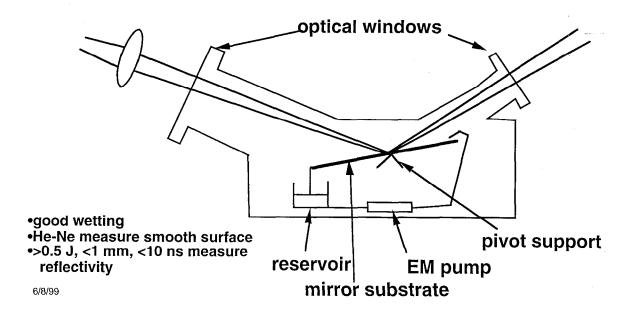


Fig. 18. Schematic of experiment to test the GILMM concept.

Conclusion

A thin liquid metal film of ~100 µm thickness flowing down an inclined plane can form a smooth surface for use as the final optical element for laser fusion. This reflective mirror should have long service life and can stand bursts of neutrons, debris and x rays from fusion microexplosions. The next optical element being out of the direct line of sight of the microexplosions can use coated dielectric optics, diffractive optics, or what ever optics is in use in non radiation environments. The allowed intensity on the mirror at 85° from normal incidence is predicted to be 9.3, 5, and 0.7 J/cm² for aluminum, sodium and lithium, which is 106, 57, and 7.7 J/cm² normal to the beam for aluminum, sodium and lithium. Environmental acoustic vibrations may present some problem because they can couple to standing waves on the film. Non uniform laser heating is not predicted to lead to ripples. More analysis will be needed to determine feasibility of the concept and to chose which liquid metal best meets the IFE requirements. Experimental verification of the GILMM idea is recommended.

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